#### **Digital Image Processing**

#### Image Enhancement (Spatial Filtering 2)

Course Website: http://www.comp.dit.ie/bmacnamee

#### Contents

# In this lecture we will look at more spatial filtering techniques

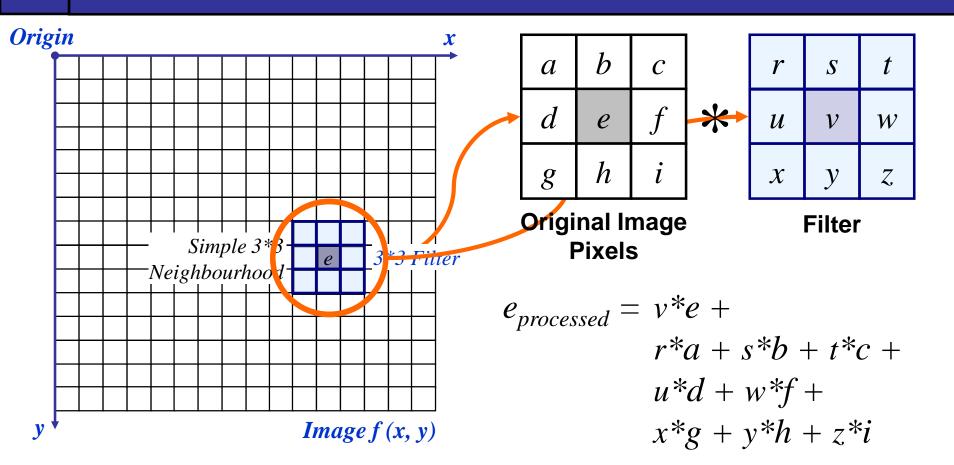
- Spatial filtering refresher
- Sharpening filters

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- 1<sup>st</sup> derivative filters
- 2<sup>nd</sup> derivative filters
- Combining filtering techniques

## **Spatial Filtering Refresher**



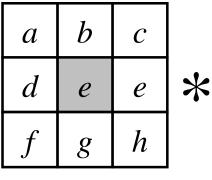
The above is repeated for every pixel in the original image to generate the smoothed image

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# **Correlation & Convolution**

•The filtering we have been talking about so far is referred to as *correlation* with the filter itself referred to as the *correlation kernel* 

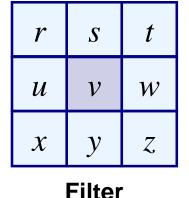
•*Convolution* is a similar operation, with just one subtle difference



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Original Image Pixels

 $e_{processed} = v^*e + z^*a + y^*b + x^*c + w^*d + u^*e + t^*f + s^*g + r^*h$ 

For symmetric filters it makes no difference

# **Correlation & Convolution**

 Correlation and Convolution are basic operations that we will perform to extract information from images.

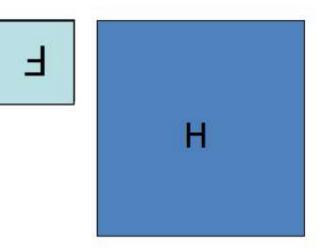
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- Cross-correlation means sliding a kernel (filter) across an image.
- Convolution means sliding a flipped kernel across an image

#### Convolution

 $G = H \underset{\uparrow}{\star} F$ Notation for convolution operator



Previously we have looked at smoothing filters which remove fine detail

Sharpening spatial filters seek to highlight fine detail

- Remove blurring from images
- Highlight edges

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Sharpening filters are based on *spatial differentiation* 

## **Spatial Differentiation**

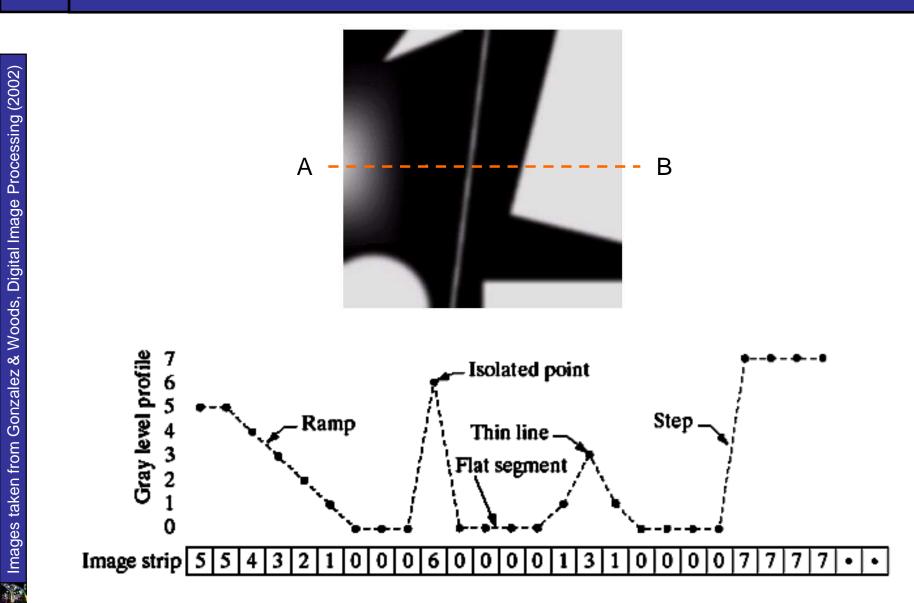
# Differentiation measures the *rate of change* of a function

# Let's consider a simple 1 dimensional example





## **Spatial Differentiation**



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#### 1<sup>st</sup> Derivative

The formula for the 1<sup>st</sup> derivative of a function is as follows:

$$\frac{\partial f}{\partial x} = f(x+1) - f(x)$$

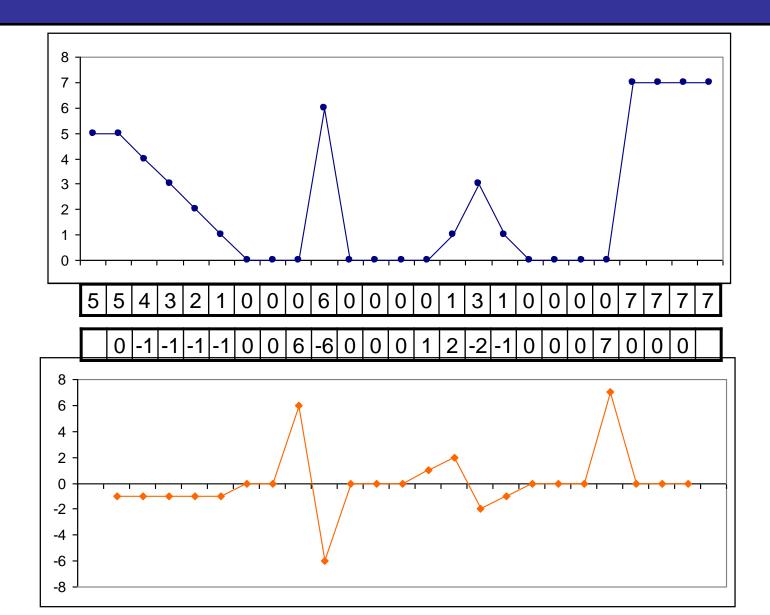
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It's just the difference between subsequent values and measures the rate of change of the function

# 1<sup>st</sup> Derivative (cont...)



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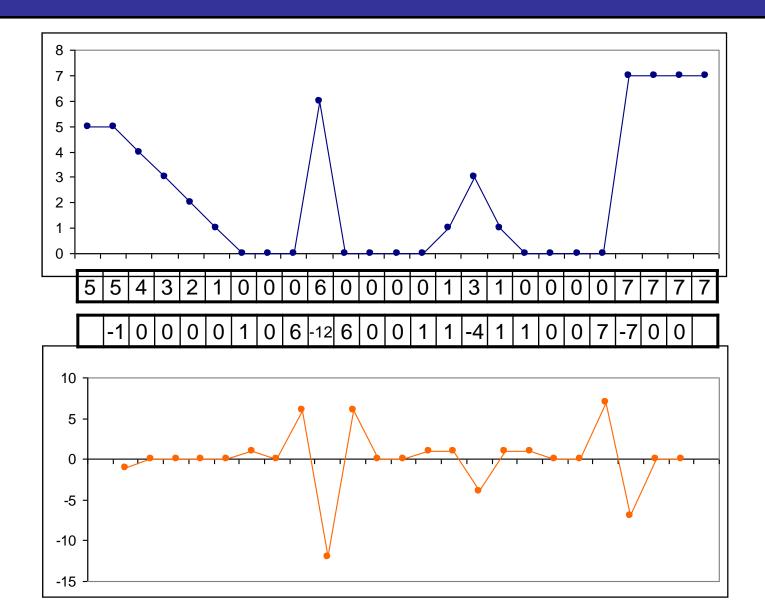
#### 2<sup>nd</sup> Derivative

The formula for the 2<sup>nd</sup> derivative of a function is as follows:

$$\frac{\partial^2 f}{\partial^2 x} = f(x+1) + f(x-1) - 2f(x)$$

Simply takes into account the values both before and after the current value

# 2<sup>nd</sup> Derivative (cont...)



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The 2<sup>nd</sup> derivative is more useful for image enhancement than the 1<sup>st</sup> derivative

- Stronger response to fine detail
- Simpler implementation
- We will come back to the 1<sup>st</sup> order derivative later on

The first sharpening filter we will look at is the *Laplacian* 

- Isotropic
- One of the simplest sharpening filters
- We will look at a digital implementation

### The Laplacian

The Laplacian is defined as follows:

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$$\nabla^2 f = \frac{\partial^2 f}{\partial^2 x} + \frac{\partial^2 f}{\partial^2 y}$$

where the partial  $1^{st}$  order derivative in the x direction is defined as follows:

$$\frac{\partial^2 f}{\partial^2 x} = f(x+1, y) + f(x-1, y) - 2f(x, y)$$
  
and in the *y* direction as follows:

$$\frac{\partial^2 f}{\partial^2 y} = f(x, y+1) + f(x, y-1) - 2f(x, y)$$

So, the Laplacian can be given as follows:

$$\nabla^2 f = [f(x+1, y) + f(x-1, y) + f(x, y-1)] + f(x, y+1) + f(x, y-1)] - 4f(x, y)$$

We can easily build a filter based on this

0	1	0
1	-4	1
0	1	0

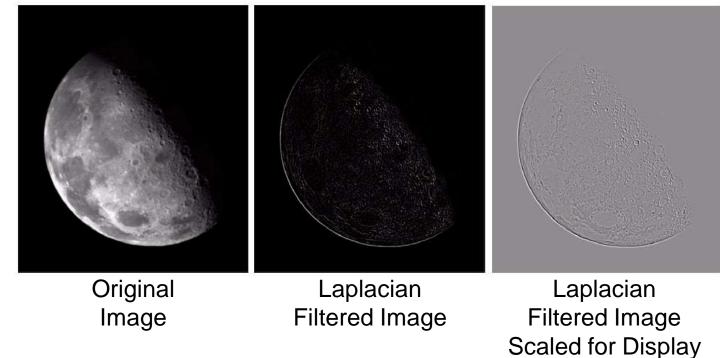
# The Laplacian (cont...)

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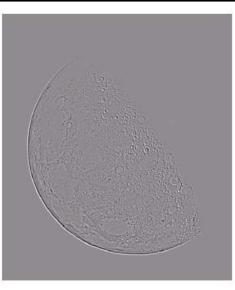
# Applying the Laplacian to an image we get a new image that highlights edges and other discontinuities



# But That Is Not Very Enhanced!

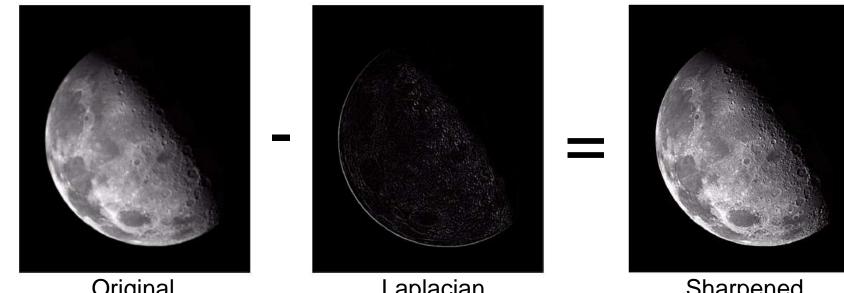
The result of a Laplacian filtering is not an enhanced image We have to do more work in order to get our final image Subtract the Laplacian result from the original image to generate our final sharpened enhanced image

$$g(x, y) = f(x, y) - \nabla^2 f$$



Laplacian Filtered Image Scaled for Display

# Laplacian Image Enhancement



Original Image Laplacian Filtered Image

Sharpened Image

In the final sharpened image edges and fine detail are much more obvious

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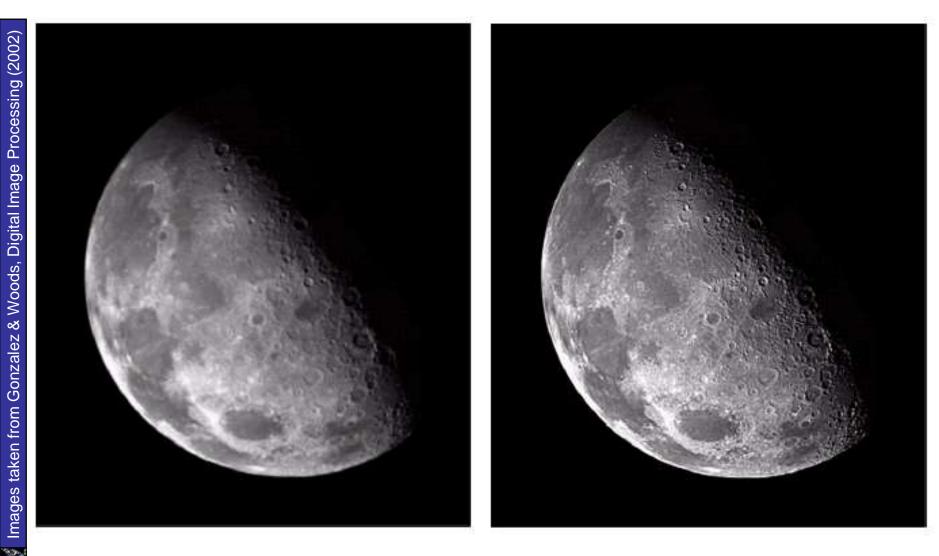
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# Laplacian Image Enhancement

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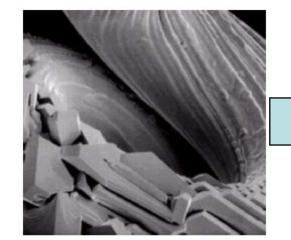
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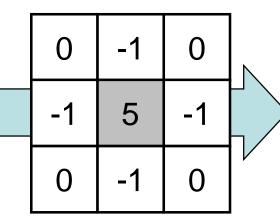
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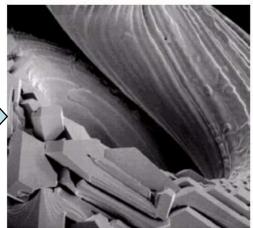
The entire enhancement can be combined into a single filtering operation  $g(x, y) = f(x, y) - \nabla^2 f$ = f(x, y) - [f(x+1, y) + f(x-1, y)]+ f(x, y+1) + f(x, y-1)-4f(x, y)] =5f(x, y) - f(x+1, y) - f(x-1, y)-f(x, y+1) - f(x, y-1)

## Simplified Image Enhancement (cont...)

# This gives us a new filter which does the whole job for us in one step



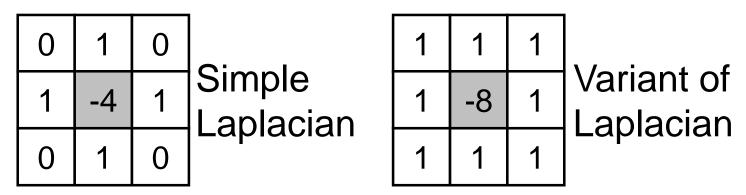


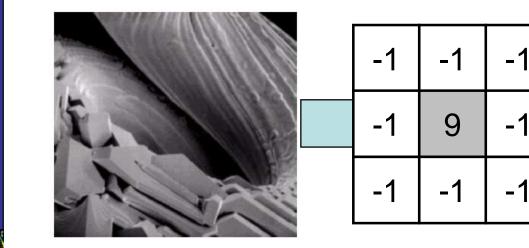


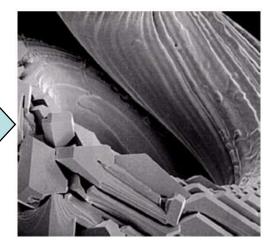
## Simplified Image Enhancement (cont...)

# Variants On The Simple Laplacian

There are lots of slightly different versions of the Laplacian that can be used:





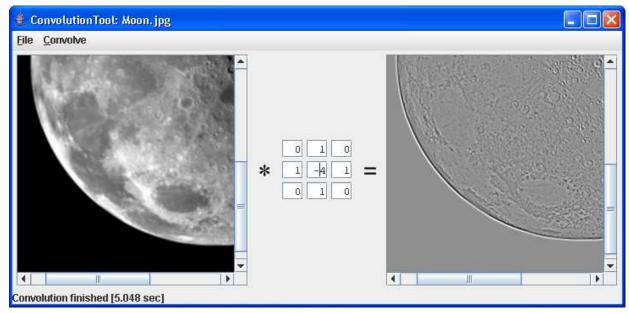


A great tool for testing out different filters

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- From the book "Image Processing tools in Java"
- Available from webCT later on today
- To launch: java ConvolutionTool Moon.jpg



Implementing 1<sup>st</sup> derivative filters is difficult in practice

For a function f(x, y) the gradient of f at coordinates (x, y) is given as the column vector:

$$\nabla \mathbf{f} = \begin{bmatrix} G_x \\ G_y \end{bmatrix} = \begin{bmatrix} \frac{\partial f}{\partial x} \\ \frac{\partial f}{\partial y} \end{bmatrix}$$

26 of 30 The magnitude of this vector is given by:

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$$\nabla f = mag(\nabla f)$$
$$= \left[ G_x^2 + G_y^2 \right]^{\frac{1}{2}}$$
$$= \left[ \left( \frac{\partial f}{\partial x} \right)^2 + \left( \frac{\partial f}{\partial y} \right)^2 \right]^{\frac{1}{2}}$$

For practical reasons this can be simplified as:  $\nabla f \approx |G_x| + |G_y|$  There is some debate as to how best to calculate these gradients but we will use:  $\nabla f \approx |(z_7 + 2z_8 + z_9) - (z_1 + 2z_2 + z_3)|$  $+ |(z_3 + 2z_6 + z_9) - (z_1 + 2z_4 + z_7)|$ 

which is based on these coordinates

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Z <sub>1</sub>	Z <sub>2</sub>	Z <sub>3</sub>
<b>Z</b> <sub>4</sub>	Z <sub>5</sub>	Z <sub>6</sub>
Z <sub>7</sub>	Z <sub>8</sub>	Z <sub>9</sub>

### **Sobel Operators**

Based on the previous equations we can derive the *Sobel Operators* 

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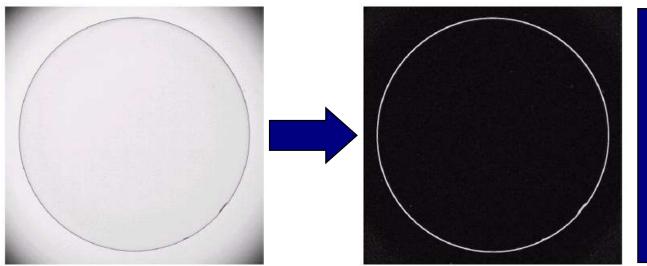
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-1	-2	-1	-1	0	1
0	0	0	-2	0	2
1	2	1	-1	0	1

To filter an image it is filtered using both operators the results of which are added together

# Sobel Example



An image of a contact lens which is enhanced in order to make defects (at four and five o'clock in the image) more obvious

# Sobel filters are typically used for edge detection

Comparing the 1<sup>st</sup> and 2<sup>nd</sup> derivatives we can conclude the following:

- 1<sup>st</sup> order derivatives generally produce thicker edges
- 2<sup>nd</sup> order derivatives have a stronger response to fine detail e.g. thin lines
- 1<sup>st</sup> order derivatives have stronger response to grey level step
- 2<sup>nd</sup> order derivatives produce a double response at step changes in grey level

### Summary

#### In this lecture we looked at:

- Sharpening filters
  - 1<sup>st</sup> derivative filters
  - 2<sup>nd</sup> derivative filters
- Combining filtering techniques

#### Combining Spatial Enhancement Methods

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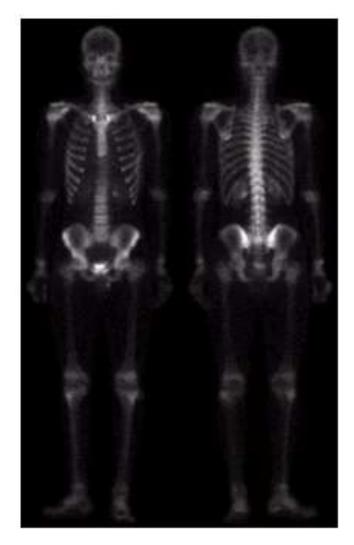
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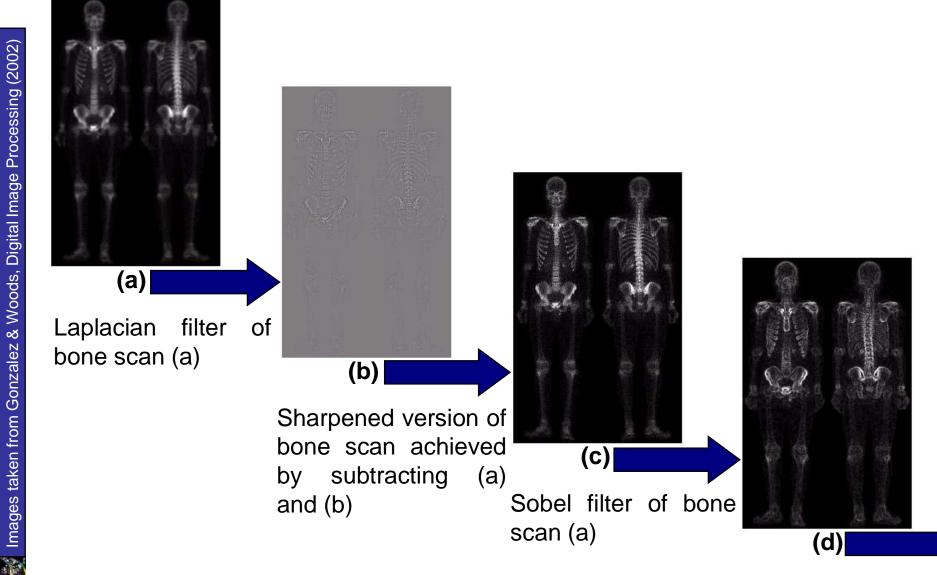
#### Successful image enhancement is typically not achieved using a single operation

#### Rather we combine a range of techniques in order to achieve a final result

This example will focus on enhancing the bone scan to the right



#### **Combining Spatial Enhancement** Methods (cont...)



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#### Combining Spatial Enhancement Methods (cont...)

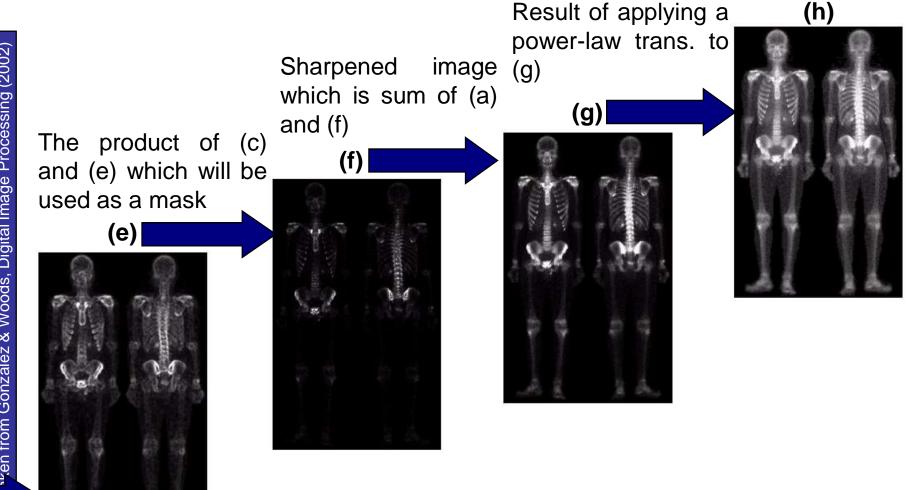


Image (d) smoothed with a 5\*5 averaging filter

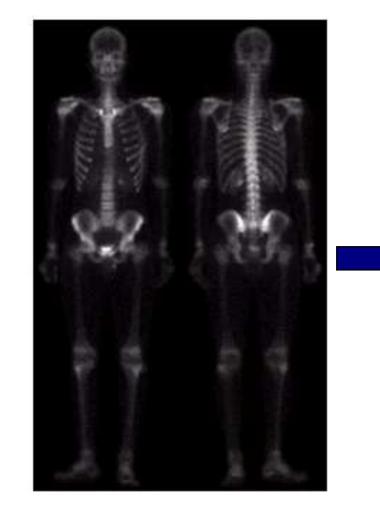
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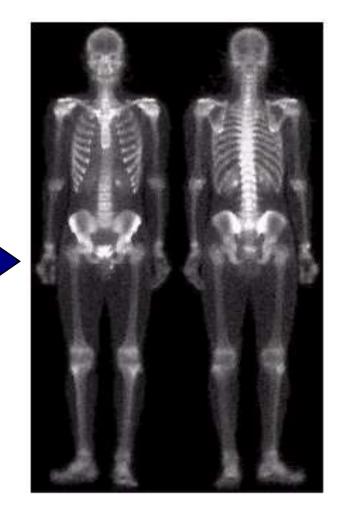
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#### Combining Spatial Enhancement Methods (cont...)

#### Compare the original and final images





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